



Computer
Science



Circuit Languages at the Confluence of Learning and Reasoning

Guy Van den Broeck

KR2ML Workshop @ NeurIPS, December 13, 2019

The AI Dilemma



Pure Logic

Pure Learning

The AI Dilemma



Pure Logic

Pure Learning

- Slow thinking: deliberative, cognitive, model-based, extrapolation
- Amazing achievements until this day
- “*Pure logic is brittle*”
noise, uncertainty, incomplete knowledge, ...



The AI Dilemma



Pure Logic

Pure Learning

- Fast thinking: instinctive, perceptive, model-free, interpolation
- Amazing achievements recently
- “*Pure learning is brittle*”
 - bias, algorithmic fairness, interpretability, explainability, adversarial attacks, unknown unknowns, calibration, verification, missing features, missing labels, data efficiency, shift in distribution, general robustness and safety
 - fails to incorporate a sensible model of the world



The **FALSE** AI Dilemma



So all hope is lost?

Probabilistic World Models

- Joint distribution $P(X)$
- Wealth of representations:
can be causal, relational, etc.
- Knowledge + data
- Reasoning + learning



Pure Logic

Probabilistic World Models

Pure Learning



**High-Level Probabilistic
Representations
Reasoning, and Learning**



Pure Logic

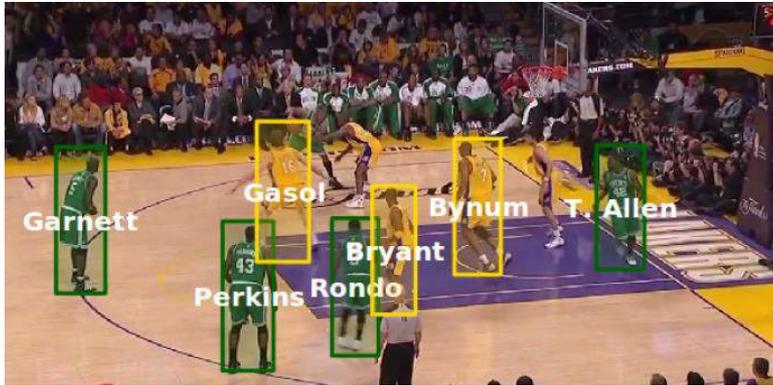
Probabilistic World Models

Pure Learning

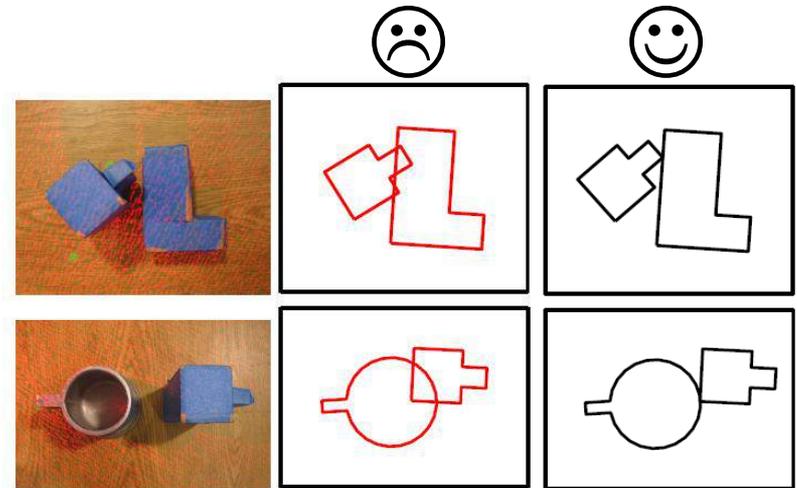


**A New Synthesis of
Learning and Reasoning**

Motivation: Vision, Robotics, NLP



People appear at most once in a frame



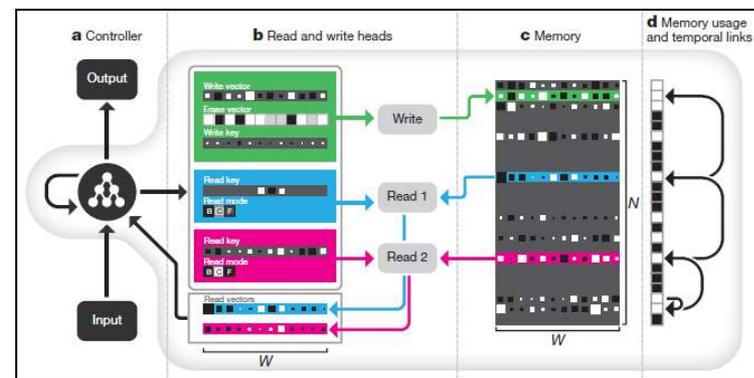
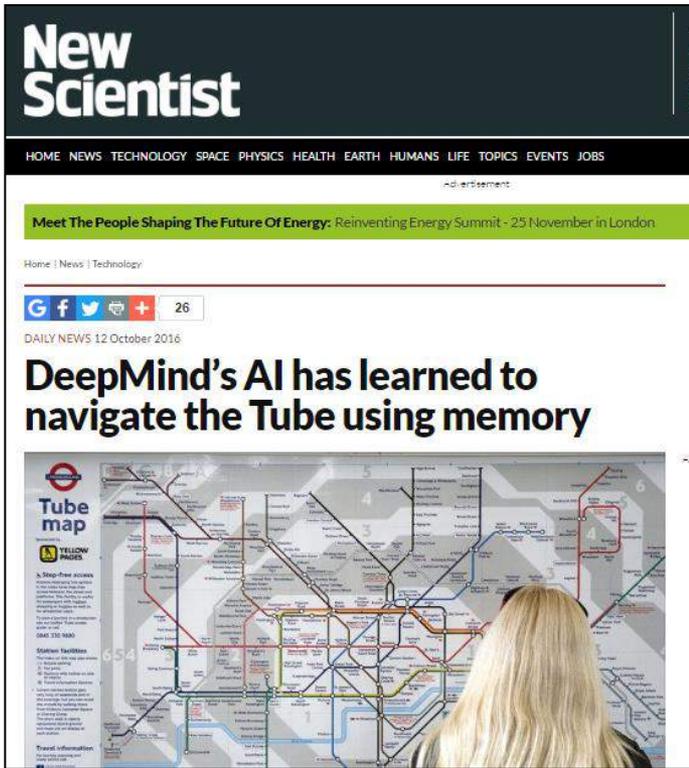
Rigid objects don't overlap

At least one verb in each sentence.

If X and Y are married, then they are people.

[Lu, W. L., Ting, J. A., Little, J. J., & Murphy, K. P. (2013). Learning to track and identify players from broadcast sports videos.], [Wong, L. L., Kaelbling, L. P., & Lozano-Perez, T., Collision-free state estimation. ICRA 2012], [Chang, M., Ratinov, L., & Roth, D. (2008). Constraints as prior knowledge], [Ganchev, K., Gillenwater, J., & Taskar, B. (2010). Posterior regularization for structured latent variable models]... and many many more!

Motivation: Deep Learning



[Graves, A., Wayne, G., Reynolds, M., Harley, T., Danihelka, I., Grabska-Barwińska, A., et al.. (2016). Hybrid computing using a neural network with dynamic external memory. *Nature*, 538(7626), 471-476.]

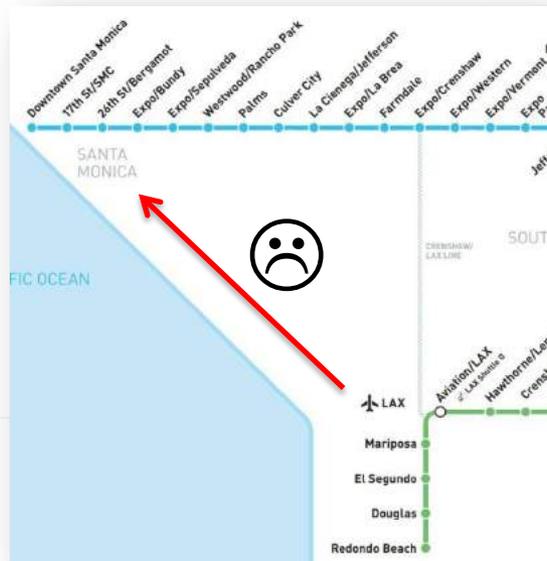
Motivation: Deep Learning

DeepMind's latest technique uses external memory to solve tasks that require **logic** and reasoning — a step toward more human-like AI.

... but ...

optimal planner recalculating a shortest path to the end node. To ensure that the network always moved to a valid node, the output distribution was renormalized over the set of possible triples outgoing from the current node. The performance

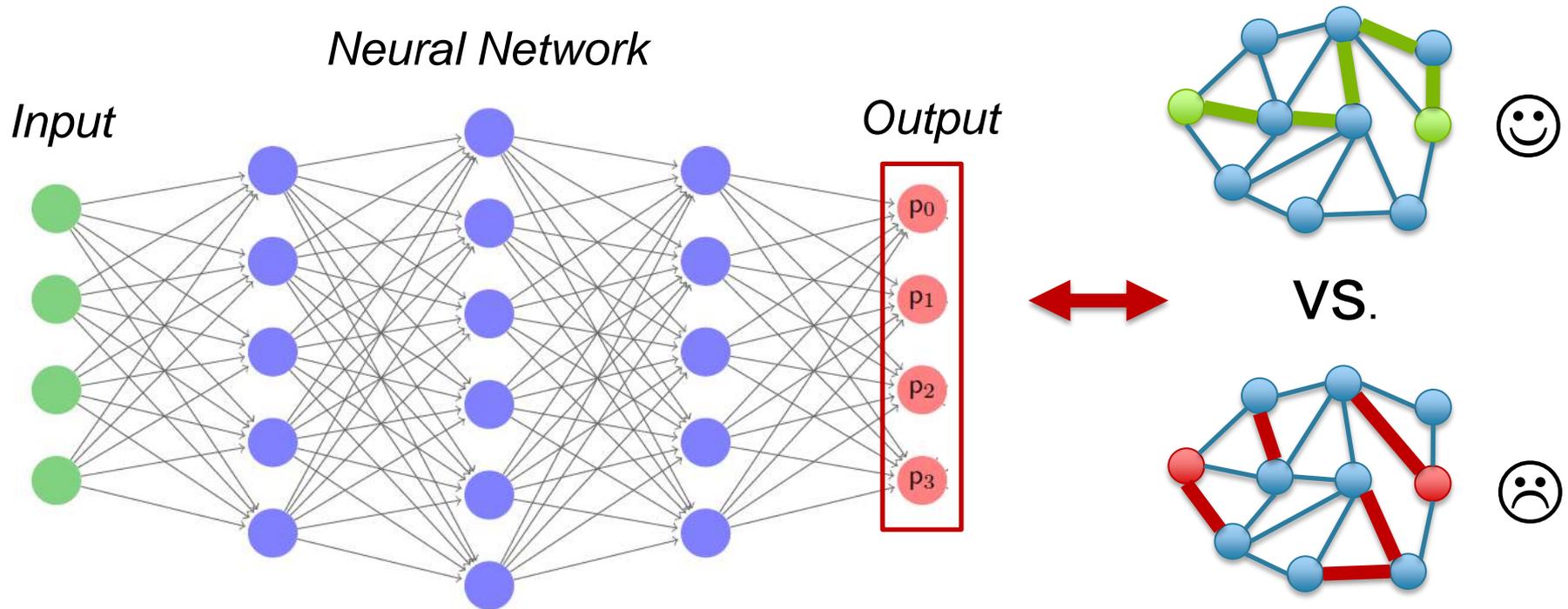
it also received input triples during the answer phase, indicating the actions chosen on the previous time-step. This makes the problem a 'structured prediction'



Knowledge vs. Data

- Where did the world knowledge go?
 - Python scripts
 - Decode/encode cleverly
 - Fix inconsistent beliefs
 - Rule-based decision systems
 - Dataset design
 - “a big hack” (with author’s permission)
- In some sense we went backwards
 - Less principled, scientific, and intellectually satisfying ways of incorporating knowledge

Deep Learning with Symbolic Knowledge



Output is probability vector p , not Boolean logic!

A Semantic Loss Function

Q: How close is output \mathbf{p} to satisfying constraint α ?

Answer: Semantic loss function $L(\alpha, \mathbf{p})$

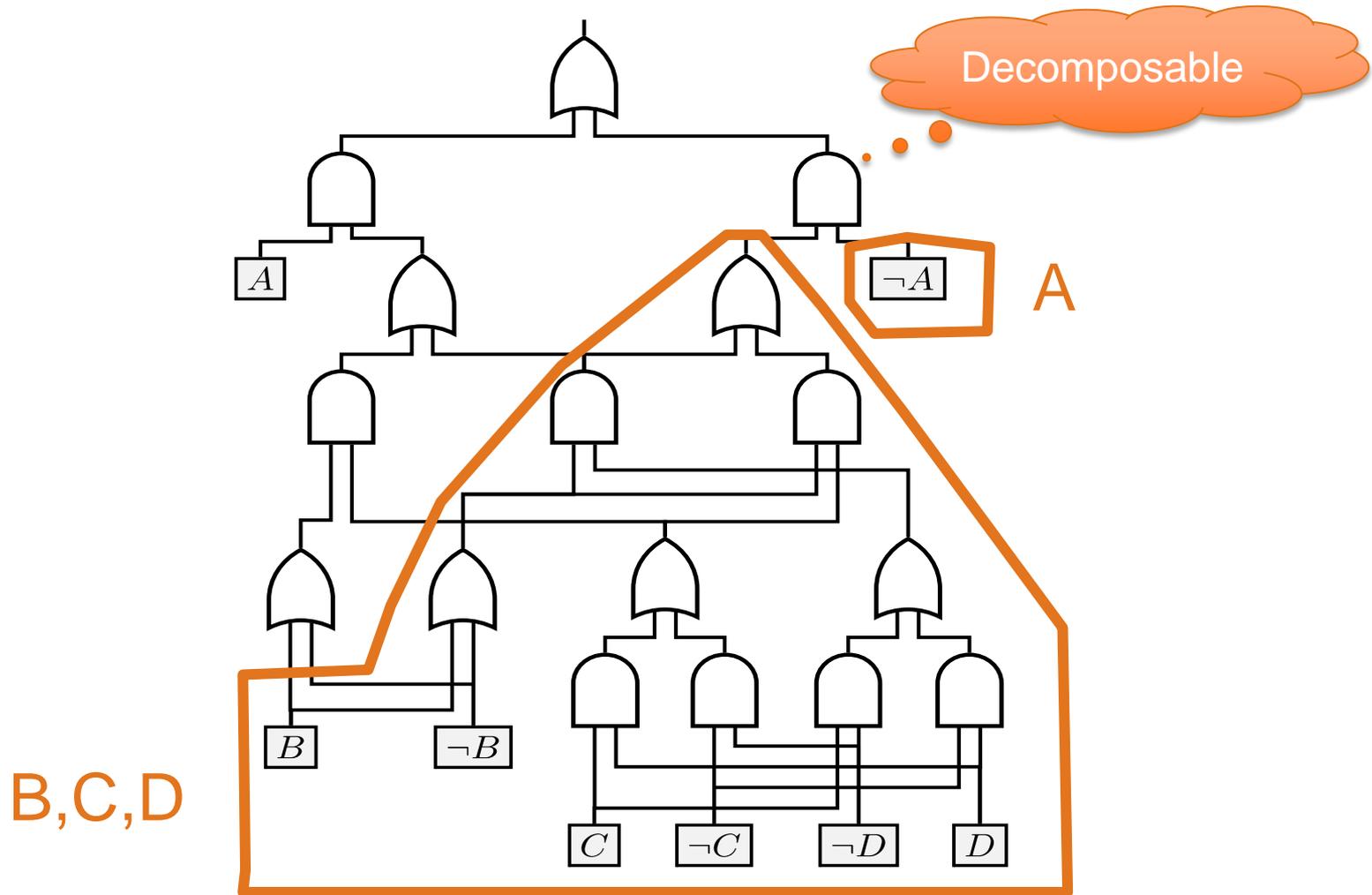
$$L^s(\alpha, \mathbf{p}) \propto -\log \underbrace{\sum_{\mathbf{x} \models \alpha} \prod_{i: \mathbf{x} \models X_i} p_i \prod_{i: \mathbf{x} \models \neg X_i} (1 - p_i)}_{\text{Probability of satisfying } \alpha \text{ after flipping coins with probabilities } \mathbf{p}}$$

How to do this reasoning during learning?

Tractable for Logical Inference

- Is there a solution? (SAT)
 - $\text{SAT}(\alpha \vee \beta)$ iff $\text{SAT}(\alpha)$ or $\text{SAT}(\beta)$ (*always*)
 - $\text{SAT}(\alpha \wedge \beta)$ iff **???**

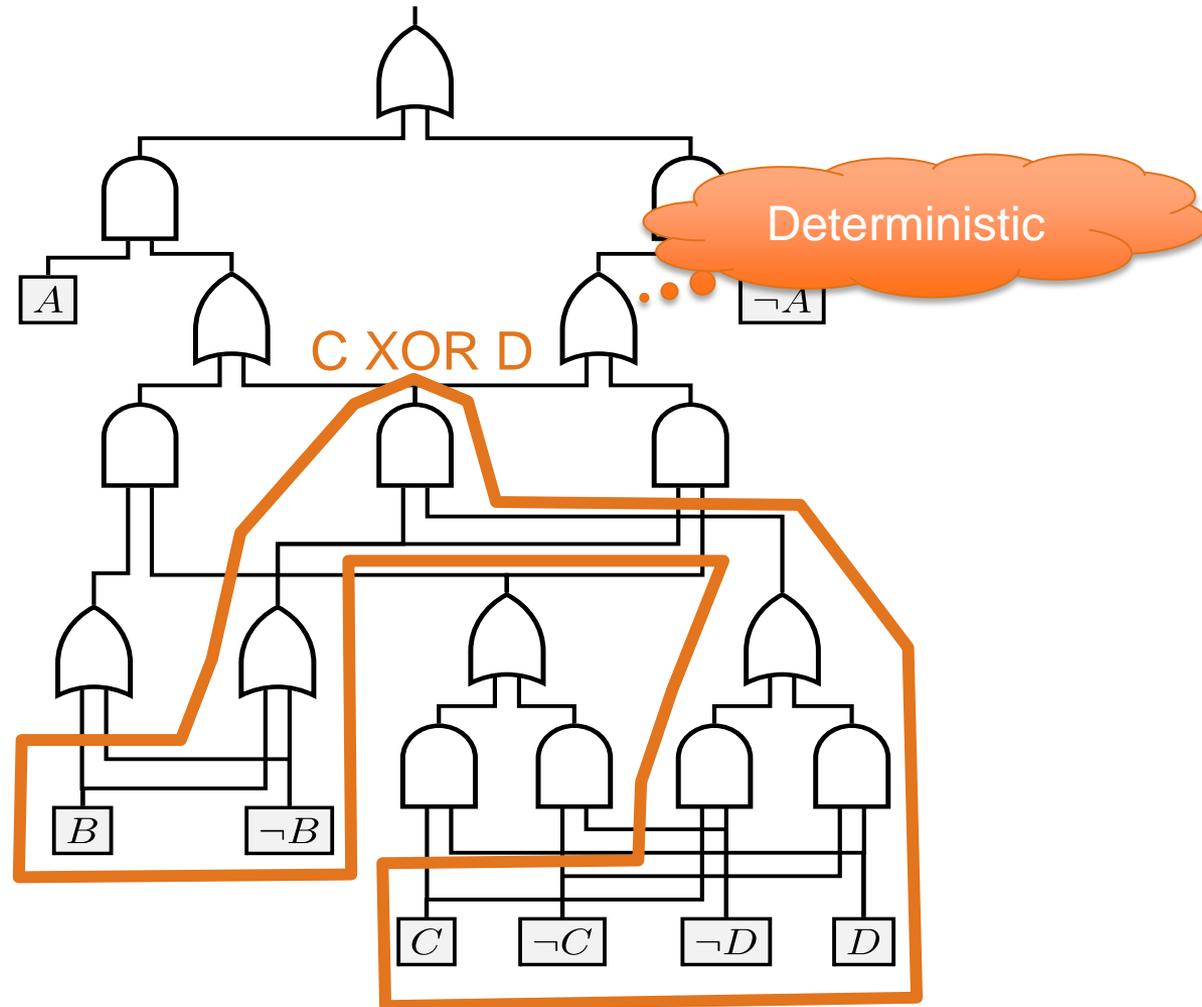
Decomposable Circuits



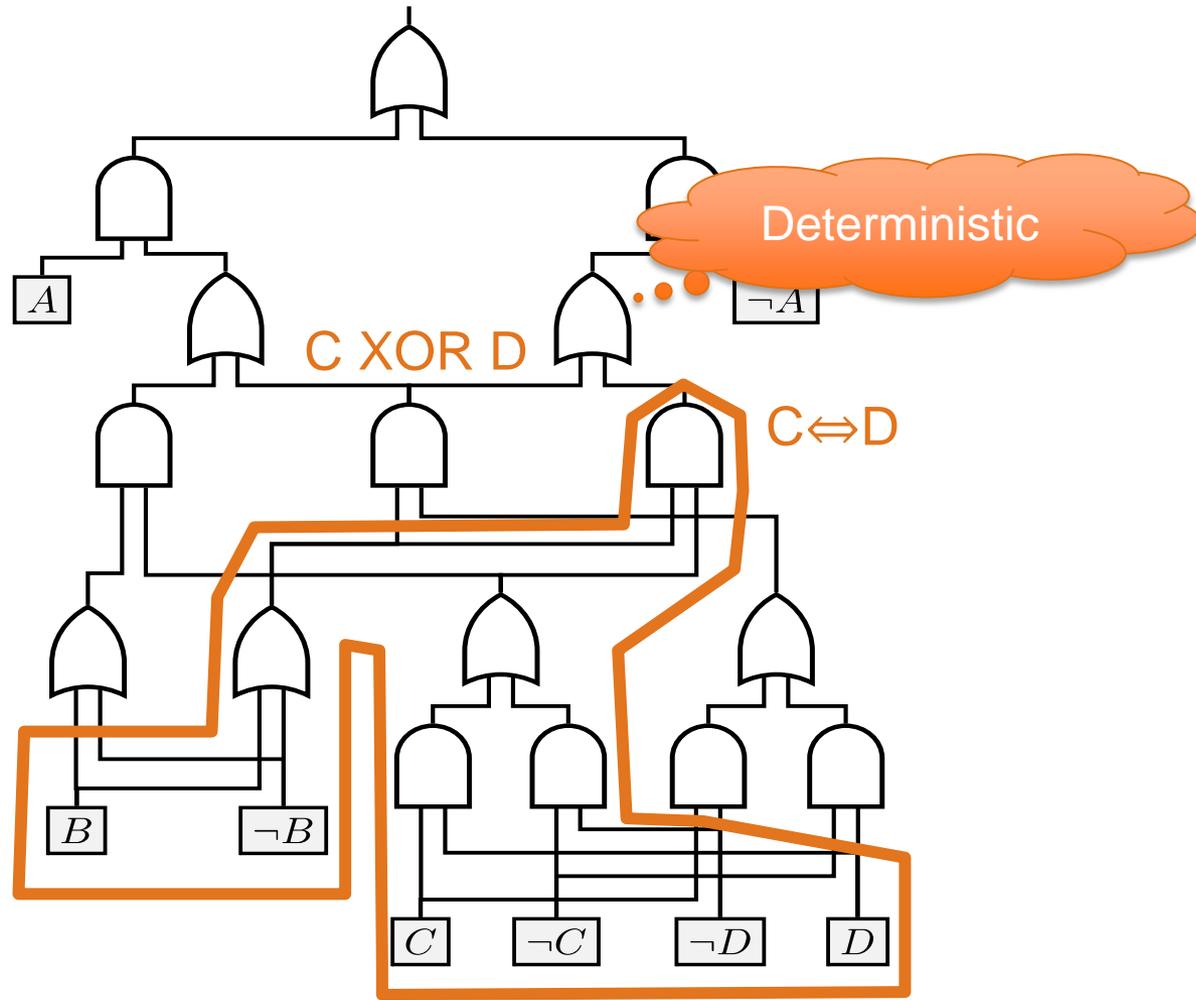
Tractable for Logical Inference

- Is there a solution? (SAT) ✓
 - $\text{SAT}(\alpha \vee \beta)$ iff $\text{SAT}(\alpha)$ or $\text{SAT}(\beta)$ (*always*)
 - $\text{SAT}(\alpha \wedge \beta)$ iff $\text{SAT}(\alpha)$ and $\text{SAT}(\beta)$ (*decomposable*)
- How many solutions are there? (#SAT)

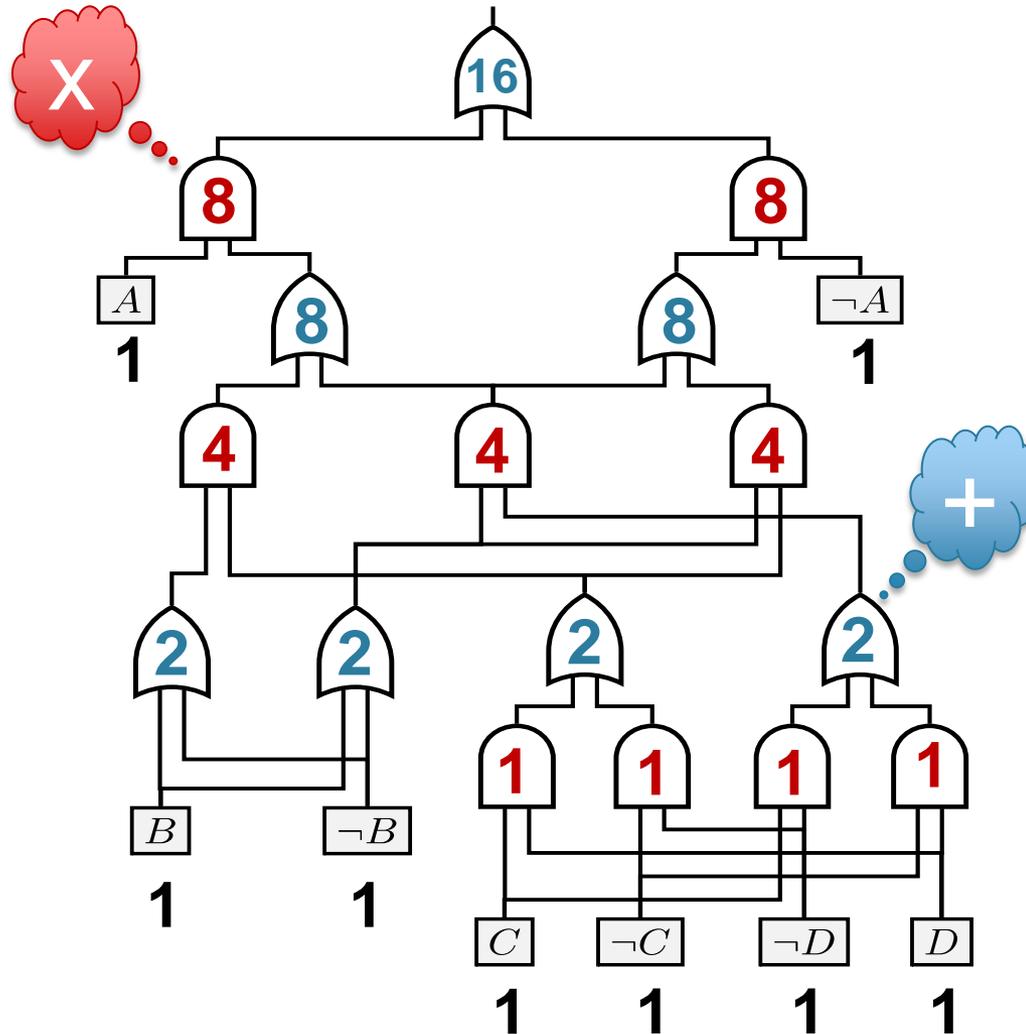
Deterministic Circuits



Deterministic Circuits



How many solutions are there? (#SAT)



Tractable for Inference

- Is there a solution? (SAT) ✓
- How many solutions are there? (#SAT) ✓
- And also semantic loss becomes tractable ✓

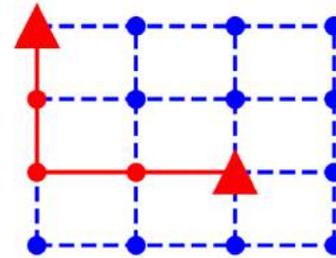
$$L(\alpha, \mathbf{p}) = L(\text{Circuit}, \mathbf{p}) = -\log(\text{Sum})$$

The diagram illustrates the conversion of a logic circuit into a probabilistic model. On the left, a logic circuit is shown with three AND gates and one OR gate. The inputs are x_1 , $\neg x_2$, $\neg x_3$, $\neg x_1$, x_2 , and x_3 . On the right, a corresponding probabilistic model is shown with three multiplication nodes (\times) and one addition node ($+$). The inputs are $\text{Pr}(x_1)$, $\text{Pr}(\neg x_2)$, $\text{Pr}(\neg x_3)$, $\text{Pr}(\neg x_1)$, $\text{Pr}(x_2)$, and $\text{Pr}(x_3)$.

- Compilation into circuit by SAT solvers
- Add circuit to neural network output in tensorflow

Predict Shortest Paths

Add semantic loss
for path constraint



Test accuracy %	Coherent	Incoherent	Constraint
5-layer MLP	5.62	85.91	6.99
Semantic loss	28.51	83.14	69.89

*Is prediction
the shortest path?*
This is the real task!

*Are individual
edge predictions
correct?*

*Is output
a path?*

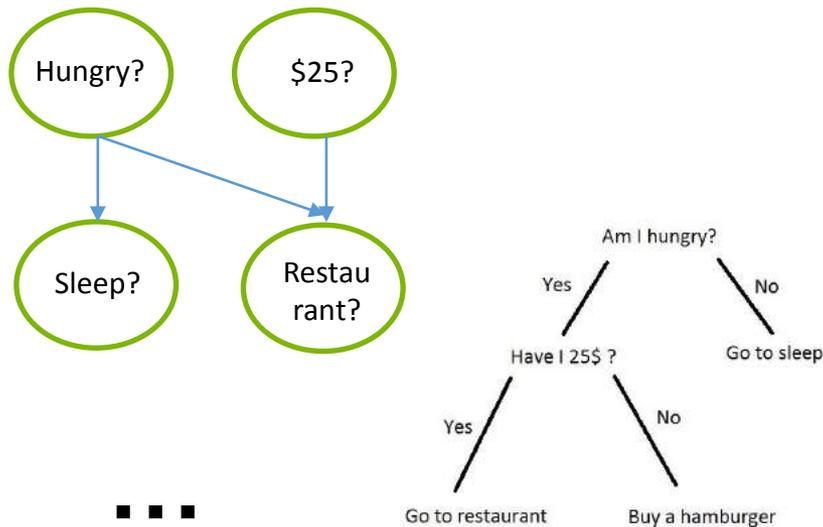
(same conclusion for predicting sushi preferences, see paper)

Early Conclusions

- Knowledge is (hidden) everywhere in ML
- Semantic loss makes logic differentiable
- Performs well semi-supervised
- Requires hard reasoning in general
 - Reasoning can be encapsulated in a circuit
 - No overhead during learning
- Performs well on structured prediction
- A little bit of reasoning goes a long way!

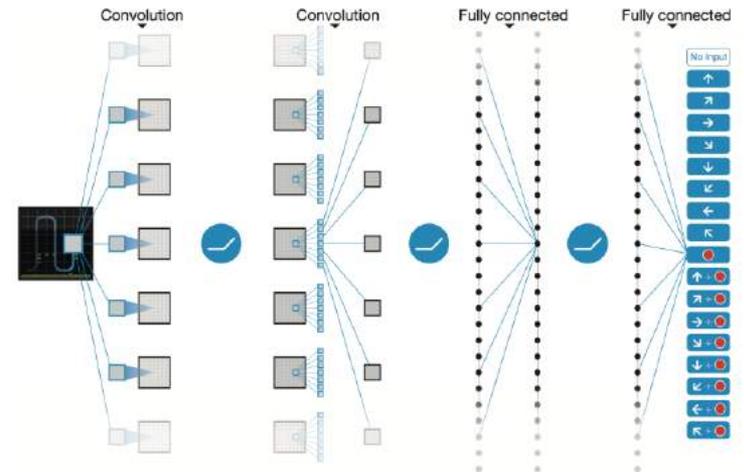
Another False Dilemma?

Classical AI Methods



Clear Modeling Assumption
Well-understood

Neural Networks



“Black Box”
Empirical performance

Probabilistic Circuits

Tractable Probabilistic Models

Representations
Inference
Learning
Applications

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July 22, 2019 - Conference on Uncertainty in Artificial Intelligence (UAI 2019) Tal Aviv

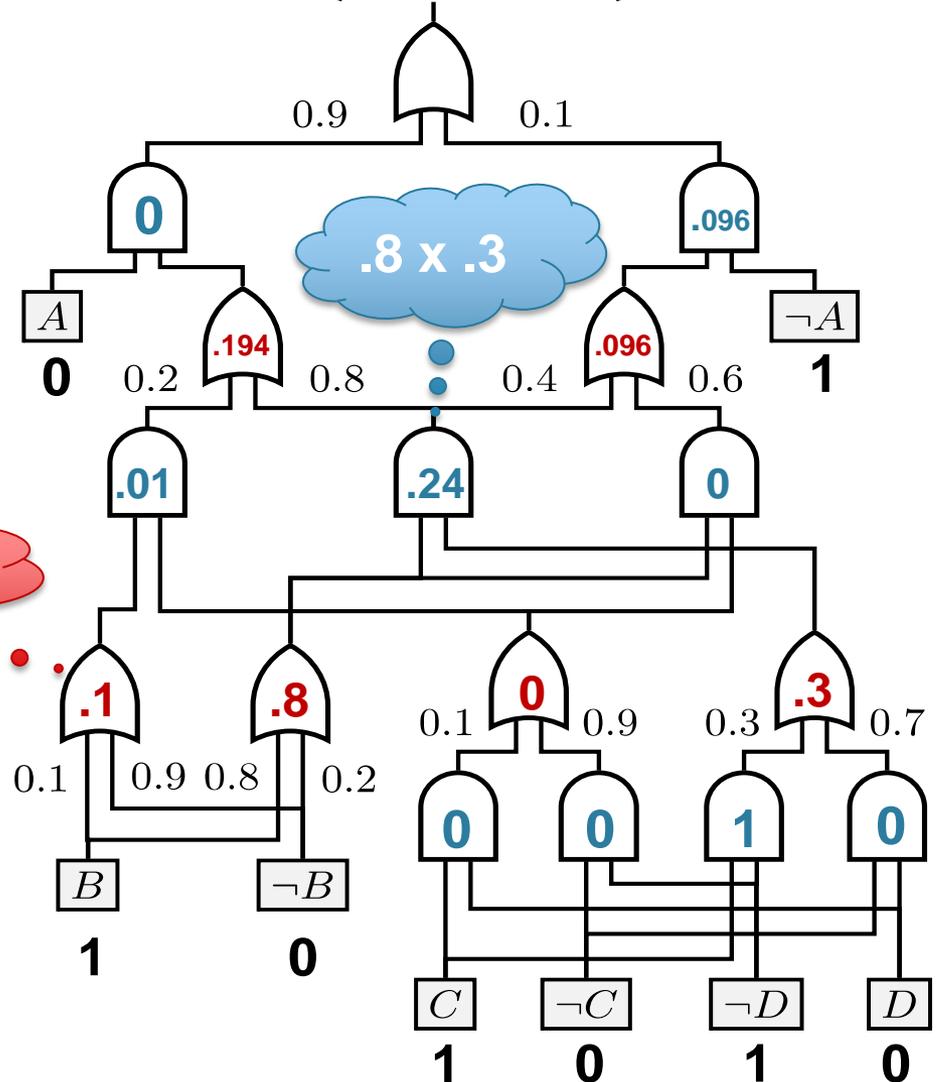
SPNs, ACs
PSDDs, CNs

$(.1 \times 1) + (.9 \times 0)$

Input:

A	B	C	D
0	1	1	0

$\Pr(A, B, C, D) = 0.096$



Properties, Properties, Properties!

- Read conditional independencies from structure
- Interpretable parameters (XAI)
(conditional probabilities of logical sentences)
- Closed-form parameter learning
- Efficient reasoning (linear 😊)
 - Computing **conditional probabilities** $\Pr(x|y)$
 - **MAP inference**: most-likely assignment to x given y
 - Even much harder tasks: expectations, KLD, entropy, logical queries, decision making queries, etc.



Probabilistic Circuits: Performance

Density estimation benchmarks: tractable vs. intractable

Dataset	<i>best circuit</i>	<i>BN</i>	<i>MADE</i>	<i>VAE</i>	Dataset	<i>best circuit</i>	<i>BN</i>	<i>MADE</i>	<i>VAE</i>
<i>nltcs</i>	-5.99	-6.02	-6.04	-5.99	<i>Book</i>	-33.82	-36.41	-33.95	-33.19
<i>msnbc</i>	-6.04	-6.04	-6.06	-6.09	<i>movie</i>	-50.34	-54.37	-48.7	-47.43
<i>kdd2000</i>	-2.12	-2.19	-2.07	-2.12	<i>webkb</i>	-149.20	-157.43	-149.59	-146.9
<i>plants</i>	-11.84	-12.65	12.32	-12.34	<i>cr52</i>	-81.87	-87.56	-82.80	-81.33
<i>audio</i>	-39.39	-40.50	-38.95	-38.67	<i>c20ng</i>	-151.02	-158.95	-153.18	-146.90
<i>jester</i>	-51.29	-51.07	-52.23	-51.54	<i>bbc</i>	-229.21	-257.86	-242.40	-240.94
<i>netflix</i>	-55.71	-57.02	-55.16	-54.73	<i>ad</i>	-14.00	-18.35	-13.65	-18.81
<i>accidents</i>	-26.89	-26.32	-26.42	-29.11					
<i>retail</i>	-10.72	-10.87	-10.81	-10.83					
<i>pumbs*</i>	-22.15	-21.72	-22.3	-25.16					
<i>dna</i>	-79.88	-80.65	-82.77	-94.56					
<i>Kosarek</i>	-10.52	-10.83	-	-10.64					
<i>Msweb</i>	-9.62	-9.70	-9.59	-9.73					

**Tractable
Probabilistic
Models**

**Representations
Inference
Learning
Applications**

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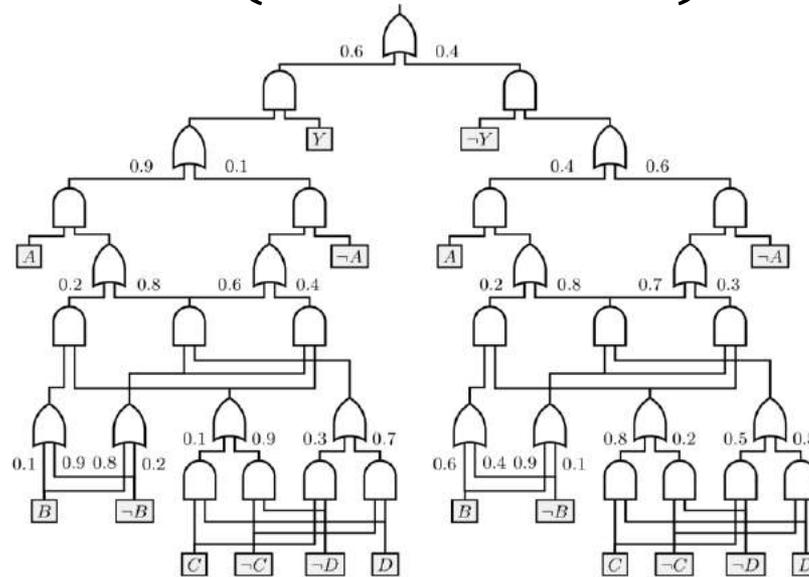
Nicola Di Mauro
University of Bari

Guy Van den Broeck
University of California, Los Angeles

But what if I only want to classify?

$$\Pr(Y|A, B, C, D)$$

~~$$\Pr(Y, A, B, C, D)$$~~



Learn a logistic circuit from data

Comparable Accuracy with Neural Nets

ACCURACY % ON DATASET	MNIST	FASHION
BASELINE: LOGISTIC REGRESSION	85.3	79.3
BASELINE: KERNEL LOGISTIC REGRESSION	97.7	88.3
RANDOM FOREST	97.3	81.6
3-LAYER MLP	97.5	84.8
RAT-SPN (PEHARZ ET AL. 2018)	98.1	89.5
SVM WITH RBF KERNEL	98.5	87.8
5-LAYER MLP	99.3	89.8
LOGISTIC CIRCUIT (BINARY)	97.4	87.6
LOGISTIC CIRCUIT (REAL-VALUED)	99.4	91.3
CNN WITH 3 CONV LAYERS	99.1	90.7
RESNET (HE ET AL. 2016)	99.5	93.6

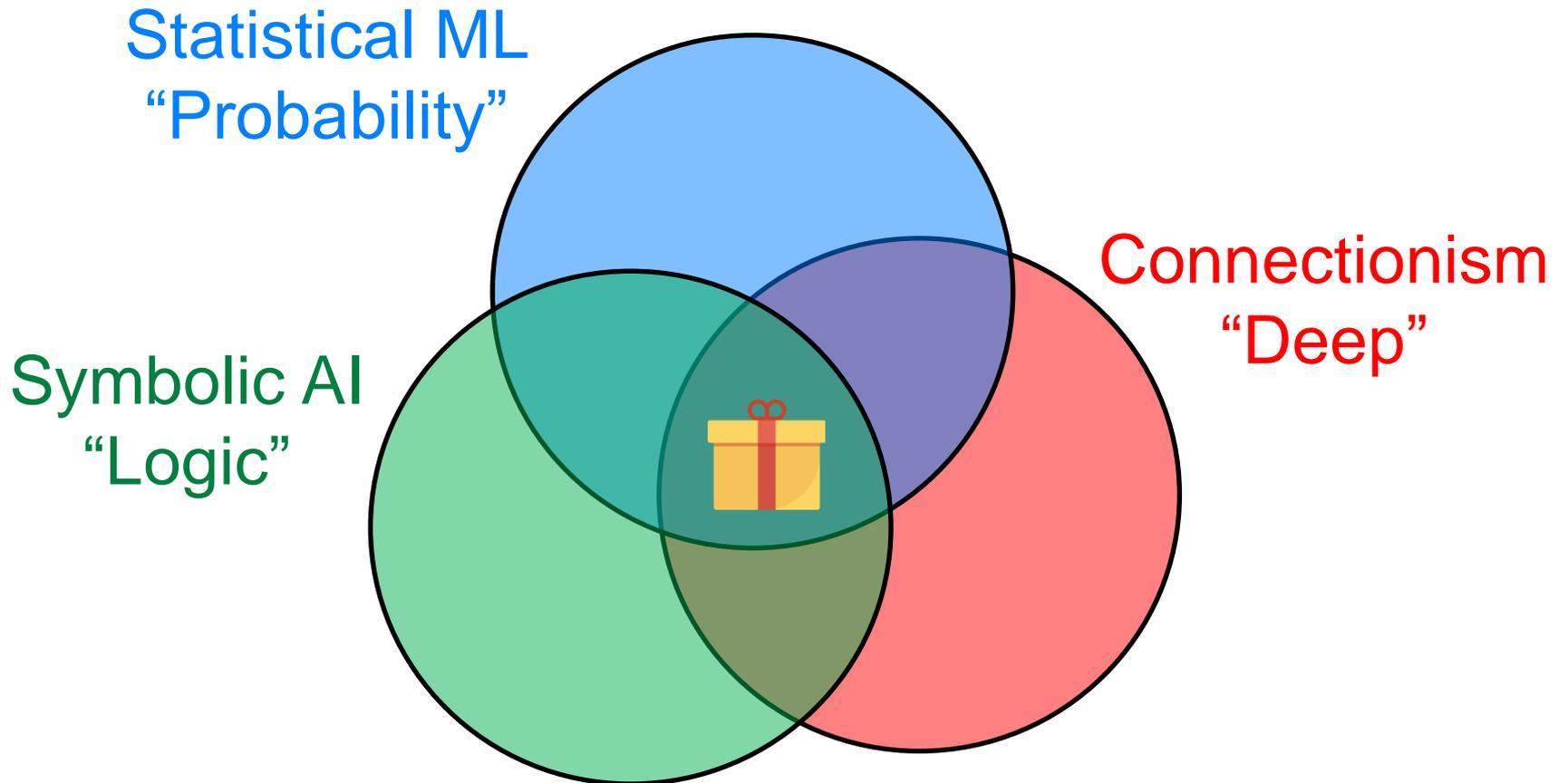
Significantly Smaller in Size

NUMBER OF PARAMETERS	MNIST	FASHION
BASELINE: LOGISTIC REGRESSION	<1K	<1K
BASELINE: KERNEL LOGISTIC REGRESSION	1,521 K	3,930K
LOGISTIC CIRCUIT (REAL-VALUED)	182K	467K
LOGISTIC CIRCUIT (BINARY)	268K	614K
3-LAYER MLP	1,411K	1,411K
RAT-SPN (PEHARZ ET AL. 2018)	8,500K	650K
CNN WITH 3 CONV LAYERS	2,196K	2,196K
5-LAYER MLP	2,411K	2,411K
RESNET (HE ET AL. 2016)	4,838K	4,838K

Better Data Efficiency

ACCURACY % WITH % OF TRAINING DATA	MNIST			FASHION		
	100%	10%	2%	100%	10%	2%
5-LAYER MLP	99.3	98.2	94.3	89.8	86.5	80.9
CNN WITH 3 CONV LAYERS	99.1	98.1	95.3	90.7	87.6	83.8
LOGISTIC CIRCUIT (BINARY)	97.4	96.9	94.1	87.6	86.7	83.2
LOGISTIC CIRCUIT (REAL-VALUED)	99.4	97.6	96.1	91.3	87.8	86.0

Probabilistic & Logistic Circuits



Reasoning about World Model + Classifier

“Pure learning is brittle”

bias, algorithmic fairness, interpretability, explainability, adversarial attacks, unknown unknowns, calibration, verification, missing features, missing labels, data efficiency, shift in distribution, general robustness and safety

fails to incorporate a sensible model of the world



- Given a learned predictor $F(x)$
- Given a probabilistic world model $P(x)$
- How does the world act on learned predictors?

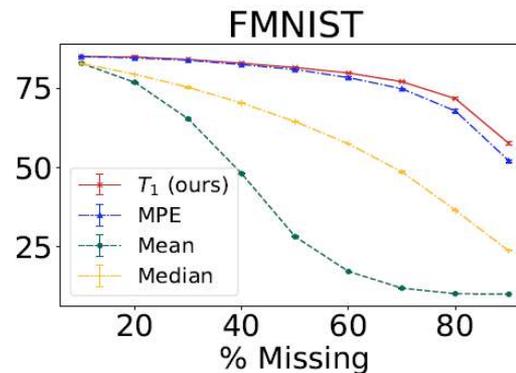
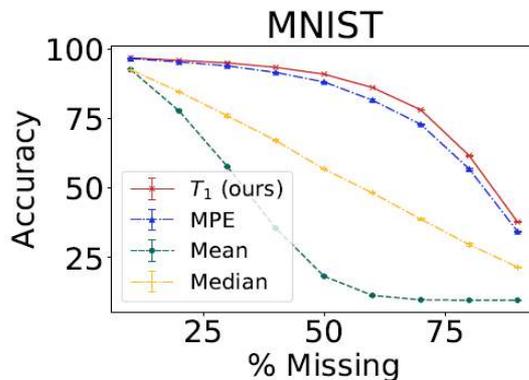
Can we solve these hard problems?

What to expect of classifiers?

- Missing features at prediction time
- What is expected prediction of $F(x)$ in $P(x)$?

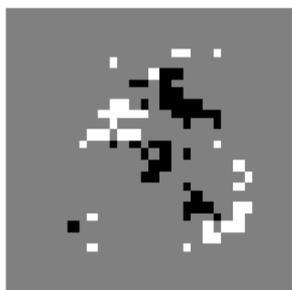
$$E_{\mathcal{F},P}(\mathbf{y}) = \mathbb{E}_{\mathbf{m} \sim P(\mathbf{M}|\mathbf{y})} [\mathcal{F}(\mathbf{y}\mathbf{m})]$$

M: Missing features
y: Observed Features



Explaining classifiers on the world

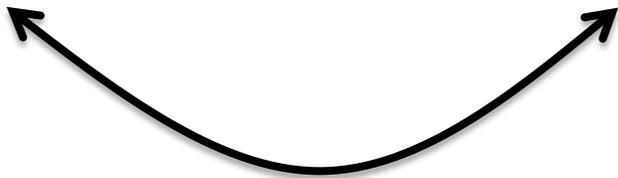
If the world looks like $P(x)$,
then what part of the data is *sufficient* for
 $F(x)$ to make the prediction it makes?



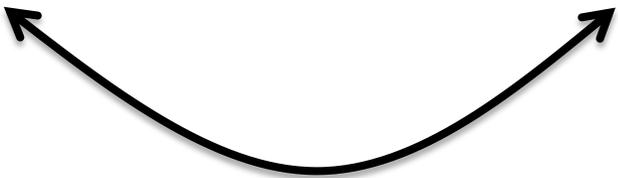
Conclusions



Pure Logic **Probabilistic World Models** **Pure Learning**



Bring high-level representations, general knowledge, and efficient high-level reasoning to probabilistic models
(*Weighted Model Integration, Probabilistic Programming*)



Bring back models of the world, supporting new tasks, and reasoning about what we have learned, without compromising learning performance

Conclusions

- There is a lot of value in working on pure logic, pure learning
- But we can do more by finding a synthesis, a confluence

Let's get rid of this false dilemma...

Advertisements

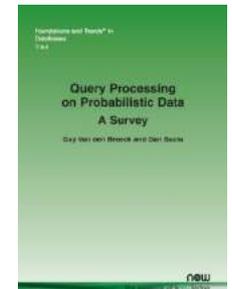
- *Juice.jl* library for circuits and ML
 - Structure and parameter learning algorithms
 - Advanced reasoning algorithms with probabilistic and logical circuits
 - Scalable implementation in Julia (release this month)
- Special Session for KR & ML
 - Knowledge Representation and Reasoning (KR 2020)
 - Submit in March! Go to Rhodes, Greece.



Thanks

References

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- **Probabilistic databases**
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- **Weighted model integration**
Vaishak Belle, Andrea Passerini and Guy Van den Broeck. [Probabilistic Inference in Hybrid Domains by Weighted Model Integration](#), *In Proceedings of 24th International Joint Conference on Artificial Intelligence (IJCAI)*, 2015.



References

- **Probabilistic circuits**
Antonio Vergari, Nicola Di Mauro and Guy Van den Broeck. [Tractable Probabilistic Models](#), UAI Tutorial, 2019.
- **Logistic circuits**
Yitao Liang and Guy Van den Broeck. [Learning Logistic Circuits](#), *In Proceedings of the 33rd Conference on Artificial Intelligence (AAAI)*, 2019.
- **What to expect of classifiers?**
Pasha Khosravi, Yitao Liang, YooJung Choi and Guy Van den Broeck. [What to Expect of Classifiers? Reasoning about Logistic Regression with Missing Features](#), *In Proceedings of the ICML Workshop on Tractable Probabilistic Modeling (TPM)*, 2019.
& unpublished work in progress

